

Statistics

Lecture 8



Feb 19-8:47 AM

8 new people were hired.

SG 13

4 Morning, 3 afternoon, and 1 night shift.

5 Females & 3 Males.

Focus on afternoon shift.

$$1) P(\text{all females}) = \frac{5}{8} \cdot \frac{4}{7} \cdot \frac{3}{6} = \frac{5}{28}$$

$$2) P(\text{all males}) = \frac{3}{8} \cdot \frac{2}{7} \cdot \frac{1}{6} = \frac{1}{56}$$

$$3) P(\text{are Same gender}) = P(\text{FFF or MMM})$$

$$= \frac{5}{28} + \frac{1}{56} = \frac{11}{56}$$

$$4) P(\text{not Same gender}) = P(\text{Same gender})$$

$$= 1 - P(\text{Same gender})$$

$$= 1 - \frac{11}{56} = \frac{45}{56}$$

Oct 17-11:36 AM

5) $P(\text{at least 1 Female})$ 

$$= 1 - P(\text{No Females})$$

$$= 1 - P(\text{all Male})$$

$$= 1 - \frac{1}{56} = \boxed{\frac{55}{56}}$$

6) $P(\text{at least 1 male}) = 1 - P(\text{No males})$ 

$$= 1 - P(\text{All Females})$$

$$= 1 - \frac{5}{28} = \boxed{\frac{23}{28}}$$

Oct 17-11:45 AM

7) $P(\text{exactly 1 Female})$

$$\begin{array}{ccc} \checkmark & \checkmark & \checkmark \\ F & M & M \end{array}$$

$$M \ F \ M$$

$$M \ M \ F$$

$$= 3 \cdot \frac{5}{8} \cdot \frac{3}{7} \cdot \frac{2}{6} = \boxed{\frac{15}{56}}$$

8) $P(\text{exactly 2 Females})$

$$\begin{array}{ccc} \checkmark & \checkmark & \checkmark \\ F & F & M \end{array}$$

$$F \ M \ F$$

$$M \ F \ F$$

$$= 3 \cdot \frac{5}{8} \cdot \frac{4}{7} \cdot \frac{3}{6} = \boxed{\frac{15}{28}}$$

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# F	P(#F)
3	5/28
2	15/28
1	15/56
0	1/56

L1 { 3, 2, 1, 0 }
 L2 { 5/28, 15/28, 15/56, 1/56 }

Clear all lists
 #F → L1
 P(#F) → L2

[STAT] [→] CALC
 [1:1-Var Stats]
 List: L1
 FreqList: L2
 [Enter]
 [Calculate]

$\bar{x} = 1.875$
 $S = S_x = \text{Blank}$
 $n = 1$

Total Prob.

Oct 17-11:55 AM

A piggy bank has 2 quarters & 3 dimes.
 take 2 coins with replacement

QQ 50¢ QD 35¢ DQ 35¢ DD 20¢

$P(50¢) = P(QQ) = \frac{2}{5} \cdot \frac{2}{5} = \frac{4}{25} = .16$
 $P(35¢) = P(QD \text{ or } DQ) = 2 \cdot \frac{2}{5} \cdot \frac{3}{5} = \frac{12}{25} = .48$
 $P(20¢) = P(DD) = \frac{3}{5} \cdot \frac{3}{5} = \frac{9}{25} = .36$

¢	P(¢)
50	.16
35	.48
20	.36

¢ → L1, P(¢) → L2
 use [1-Var Stats] with
 L1 & L2

$\bar{x} = 32$
 $S = \text{blank}$
 Total Prob. → $n = 1$

Oct 17-12:02 PM

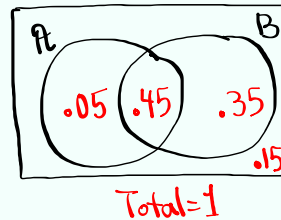
$$P(A) = .5, \quad P(B) = .8, \quad P(A \text{ and } B) = .45$$

$$1) P(\bar{B}) = 1 - P(B) \\ = \boxed{.2}$$

$$2) P(\overline{A \text{ and } B}) = 1 - .45 \\ = \boxed{.55}$$

$$3) P(A \text{ or } B) \\ = P(A) + P(B) - P(A \text{ and } B) \\ = .5 + .8 - .45 = \boxed{.85}$$

4) Construct Venn diagram.



$$5) P(B|A) = \frac{P(A \text{ and } B)}{P(A)} = \frac{.45}{.5} \\ = \boxed{.9}$$

$$6) P(A|B) = \frac{P(A \text{ and } B)}{P(B)} = \frac{.45}{.8} \approx \boxed{.563}$$

Oct 17-12:11 PM

$$P(\text{Pants}) = .4$$

$$P(\text{Shoes} \cap \text{Pants})$$

$$P(\text{Shoes}) = .5$$

$$P(\text{Pants} | \text{Shoes}) = \frac{P(\text{Shoes} \cap \text{Pants})}{P(\text{Shoes})}$$

$$P(\text{Pants} | \text{Shoes}) = .6$$

$$.6 = \frac{P(\text{Shoes} \cap \text{Pants})}{.5}$$

$$P(\text{Shoes} | \text{Pants}) = ?$$

Cross-multiply

$$= \frac{P(\text{Shoes} \cap \text{Pants})}{P(\text{Pants})}$$

$$P(\text{Shoes} \cap \text{Pants}) = (.5)(.6) \\ = \boxed{.3}$$

$$= \frac{.3}{.4} = \frac{3}{4} = \boxed{.75}$$

Oct 17-12:19 PM

$$P(A) = .5 \quad P(B) = .6 \quad P(A \text{ and } B) = .3$$

$$1) P(B | A) = \frac{P(A \text{ and } B)}{P(A)} = \frac{.3}{.5} = \frac{3}{5} = \boxed{.6}$$

$$2) P(A | B) = \frac{P(A \text{ and } B)}{P(B)} = \frac{.3}{.6} = \frac{3}{6} = \boxed{.5}$$

Independent Events

Oct 17-12:25 PM

SG 14

Data

- 1) Qualitative
- 2) Quantitative
 - 1) Discrete
 - 2) Continuous

Let x be discrete random variable with Prob. dist. $P(x)$.

Prob. dist. gives the prob. of all possible outcomes.

- 1) Table or chart
- 2) Graph
- 3) Formula
- 4) by def. of Prob.

Oct 17-12:46 PM

Some rules

1) $0 \leq P(x) \leq 1$

2) $\sum P(x) = 1$

3) $P(x) = 1 \iff \text{Sure event}$

4) $P(x) = 0 \iff \text{Impossible event}$

5) $0 < P(x) \leq .05 \iff \text{Rare event}$

Oct 17-12:50 PM

Consider the chart below

x	$P(x)$
1	.2
2	.5
3	.3

1) verify $\sum P(x) = 1$ ✓

$.2 + .5 + .3 = 1$

2) Find $P(x \leq 2)$

$.5 + .2 = .7$

3) Draw Prob. dist. histogram

$x \rightarrow \text{class MP}, P(x) \rightarrow \text{Rel. F.}$

$x \rightarrow L1, P(x) \rightarrow L2$

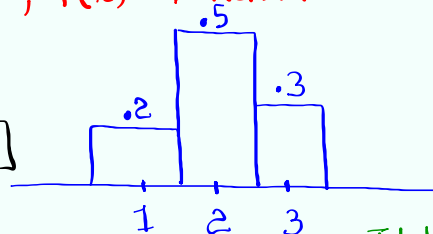
use 1-Var Stats

With $L1 \neq L2$

$\bar{x} = 2.1$

$S = S_x = \text{blank}$

$n = 1$ & Total Prob.



Oct 17-12:53 PM

Consider the chart below

x	$P(x)$
1	.2
2	.3
3	.4
4	.1

1) Find $P(X=4)$

$$= 1 - (.2 + .3 + .4)$$

$$= 1 - .9 = \boxed{.1}$$

2) Find $P(2 \leq x \leq 3)$

$$= .3 + .4 = \boxed{.7}$$

3) Draw Prob. dist. Histogram

$x \rightarrow$ class MP, $P(x) \rightarrow$ Rel. F.

$x \rightarrow$ L1, $P(x) \rightarrow$ L2

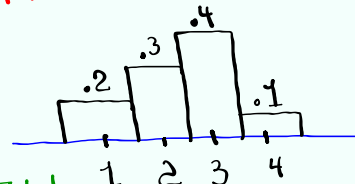
Use 1-Var Stats

with L1 \neq L2

$$\bar{x} = 2.4$$

$$S = S_x = \text{blank}$$

$$n = 1$$



Total Prob.

Oct 17-1:00 PM

A piggy bank has 2 quarters & 3 dimes.

Take 2 Coins, No replacement

QQ

50¢

QD

DQ

35¢

DD

20¢

$$P(50¢) = P(QQ) = \frac{2}{5} \cdot \frac{1}{4} = \frac{1}{10} = \boxed{.1}$$

$$P(35¢) = P(QD \text{ or } DQ) = 2 \cdot \frac{2}{5} \cdot \frac{3}{4} = \frac{3}{5} = \frac{6}{10} = \boxed{.6}$$

$$P(20¢) = P(DD) = \frac{3}{5} \cdot \frac{2}{4} = \frac{3}{10} = \boxed{.3}$$

ϕ	$P(\phi)$
50	.1
35	.6
20	.3

$\phi \rightarrow x \rightarrow$ L1

$P(\phi) \rightarrow P(x) \rightarrow$ L2

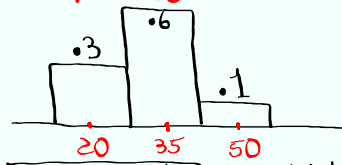
Use 1-Var Stats with L1 \neq L2

$$\bar{x} = 32$$

$$S = S_x = \text{blank}$$

$$n = 1$$

Total Prob.



Oct 17-1:06 PM

Complete the chart below

x	$P(x)$	$xP(x)$	$x^2P(x)$
1	.3	.3	.3
2	.5	1.0	2.0
3	.2	.6	1.8

1) $\sum P(x) = 1$

2) $\sum xP(x) = 1.9$

3) $\sum x^2P(x) = 4.1$

4) Compute $\sum x^2P(x) - (\sum xP(x))^2$
 $= 4.1 - 1.9^2 = .49$

5) $\sqrt{\text{Last answer}} = \sqrt{.49} = .7$

 $x \rightarrow L1$

$\bar{x} = 1.9$

 $P(x) \rightarrow L2$ Use 1-Var Stats $S = S_x = \text{blank}$

with L1 & L2

$n = 1$

Oct 17-1:18 PM

Complete the chart below

x	$P(x)$	$xP(x)$	$x^2P(x)$
1	.1	.1	.1
2	.2	.4	.8
3	.4	1.2	3.6
4	.3	1.2	4.8

1) $\sum P(x) = 1$

2) $\sum xP(x) = 2.9$

3) $\sum x^2P(x) = 9.3$

4) Compute $\sum x^2P(x) - (\sum xP(x))^2$
 $= 9.3 - 2.9^2 = .89$

5) $\sqrt{\text{Last answer}} = \sqrt{.89} \approx .943$

 $x \rightarrow L1$

$\bar{x} = 2.9$

 $P(x) \rightarrow L2$ Use 1-Var Stats $S = S_x = \text{blank}$

with L1 & L2

$n = 1$

Oct 17-1:25 PM

Working with $x \in P(x)$

Mean $\mu = \sum x p(x)$

Variance $\sigma^2 = \sum x^2 p(x) - \mu^2$

Sigma

Standard deviation $\sigma = \sqrt{\sigma^2}$

From last example

$$\mu = \sum x p(x) = 2.9$$

$$\sigma^2 = \sum x^2 p(x) - \mu^2 = .89$$

$$\sigma = \sqrt{\sigma^2} = \sqrt{.89} = .943$$

Using TI

 $x \rightarrow L1$, $P(x) \rightarrow L2$ use 1-Var Stats
with $L1 \in L2$

$$\mu = \bar{x}$$

$$\sigma = \sigma_x$$

For σ^2
VARS 5: Statistics 4: σ_x^2 x^2 Enter σ^2

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x	$P(x)$
2	.2
3	.5
4	.3

 $x \rightarrow L1$, $P(x) \rightarrow L2$ use 1-Var Stats with $L1 \in L2$

$$\mu = \bar{x} = \boxed{3.1}$$

VARS 5: Statistics
4: σ_x x^2 Enter

$$\sigma = \sigma_x = \boxed{.7}$$

$$\sigma^2 = .49$$

Oct 17-1:40 PM

family with 3 kids

 $x \rightarrow \# \text{ of boys}$ $P(x)$

x	$P(x)$
3	$\frac{1}{8}$
2	$\frac{3}{8}$
1	$\frac{3}{8}$
0	$\frac{1}{8}$

3 boys

BBB

 $\frac{1}{2}$

2 Boys

BBG

BGB

GBB

1 Boy

BGG

GBG

GGB

 $x \rightarrow L1, P(x) \rightarrow L2$ Use 1-Var Stats to find

$$\mu = 1.5$$

$$\sigma = .866$$

$$\sigma^2 = .75$$

VARS5: Statistics4: σ_x^2 x^2 Enter

Oct 17-1:43 PM

Application

Expected Value

I sold 20 tickets for \$10 each, draw 1 ticket, winner gets a Calc. worth \$100.

expected Value Per ticket

Collect $20(10)=200$

Giveaway 100

Net = \$100

$$\mu = \bar{x}$$

Net	$P(\text{Net})$
10 - 100	$\frac{1}{20}$
10 - 0	$\frac{19}{20}$

winning TKT

winning TKT

$$\frac{\$100 \text{ Net}}{20 \text{ TKTs}} = \$5/\text{TKT}$$

Net $\rightarrow L1$ $P(\text{Net}) \rightarrow L2$ 1-Var Stats with L1 & L2

$$E.V. = \mu = \bar{x} = \boxed{5}$$

Oct 17-2:00 PM

You Pay \$20 to buy a tkt

one ticket drawn

5% chance of winning a laptop (\$1000)

10% " " " a Calc. (\$100)

85% " " " nothing.

Net	P(Net)		
20-1000	.05	laptop	Net \rightarrow L1
20-100	.10	Calc.	P(Net) \rightarrow L2
20-0	.85	Nothing to give	<u>1-Var Stats</u>

$$E.V. = \mu = \bar{X}$$

house loses \$40 per ticket

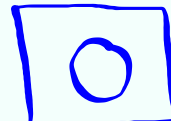
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Oct 17-2:08 PM

Pay me \$5, draw a Card from a full deck of playing cards.

IS You draw	I give you
Ace	\$50
Face	\$5
any other Card	\$0

Net	P(Net)		
5-50	4/52	Ace	Net \rightarrow L1
5-5	12/52	Face	P(Net) \rightarrow L2
5-0	36/52	any other Card	E.V. = $\mu = \bar{X}$



Oct 17-2:13 PM

Buy insurance for your luggage for \$100

Any damages, airline pays you \$1000.

Prob. of possible damages is .5%.

Find Expected Value per policy sold.

Net	P(Net)		Net $\rightarrow \Delta L1$
100 - 1000	.5% = .005	damage	P(Net) $\rightarrow \Delta L2$
100 - 0	.995	damage	1 - Var Stats



$$E.V. = \mu = \bar{x}$$

\$95

Oct 17-2:18 PM